# Decision Support System for Evaluating Transformer Investments in the Industrial Sector 

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#### Abstract

This paper presents a decision support system (DSS) for evaluating transformer investments in the industrial sector. The DSS evaluates transformer bids based on the total owning cost (TOC). Among all transformer offers, the most cost-effective and energy-efficient transformer is the one with the lowest TOC. The DSS compares the selected offer with the other competing offers. Moreover, the proposed DSS deals with the uncertainty of the values in the TOC formula by performing a sensitivity analysis.


## 1. Introduction

Transformer losses are categorized as no-load losses (NLL) and load losses (LL). No-load losses include losses due to no-load current, hysteresis losses and eddy current losses in core laminations, stray eddy current losses in core clamps and bolts and losses in the dielectric circuit. Load losses comprise losses due to load currents, losses due to current supplying the losses, and eddy current losses in conductors due to leakage fields.

Transformer efficiency is improved by reducing transformer losses. Costs for the transformer user comprise costs for the purchase of the transformer, installation, maintenance and cost of losses. An understanding of transformer economics is necessary to weigh the transformer cost against the benefits of transformer efficiency.

This paper presents a decision support system (DSS) for evaluating transformer investments in the industrial sector. The DSS evaluates transformer bids based on the total owning cost (TOC), where the TOC is defined as the first cost plus the calculated present value of future losses. Among all transformer offers, the most cost-effective and energy-efficient transformer is the one with the lowest TOC. The DSS compares the selected offer with the other competing offers. Moreover, the proposed DSS deals with the uncertainty of the values in the TOC formula by performing a sensitivity analysis.

## 2. Decision support system for transformer evaluation

In the proposed DSS, the purchasing decision is based on the minimization of the calculated TOC:

$$
\begin{equation*}
\mathrm{TOC}=\mathrm{BP}+\mathrm{A} \cdot \mathrm{NLL}+\mathrm{B} \cdot \mathrm{LL} \tag{1}
\end{equation*}
$$

where BP is the transformer bidding (purchasing) price ( $€$ ), NLL are the transformer no-load losses (W), LL are the transformer load losses (W), A is the no-load loss factor $(€ / \mathrm{W})$ and B is the load loss factor $(€ / W)$. The factors A and B are calculated as follows:

$$
\begin{gather*}
\mathrm{A}=\mathrm{PV}_{\mathrm{m}} \cdot \mathrm{EP} \cdot \mathrm{HPY} \cdot 10^{-3}  \tag{2}\\
\mathrm{~B}=\mathrm{A} \cdot \mathrm{~L}^{2} \tag{3}
\end{gather*}
$$

where $\mathrm{PV}_{\mathrm{m}}$ is the present value multiplier, EP is the electricity price $(€ / \mathrm{kWh})$, HPY are the hours of transformer operation per year (typically HPY $=8,760$ ) and L is the per unit load. The $\mathrm{PV}_{\mathrm{m}}$ is defined as $\mathrm{PV}_{\mathrm{m}}=\frac{(1+\mathrm{d})^{\mathrm{n}}-1}{\mathrm{~d} \cdot(1+\mathrm{d})^{\mathrm{n}-1}}$, where d is the discount rate and n is the transformer project life (years). The per unit load $L$ is defined as $L=S / S_{r}$, where $S$ is the transformer actual load $(k V A)$ and $S_{r}$ is the transformer rated power.

## 3. Results and discussion

Table I shows nine transformer offers for three-phase, oil-immersed, power transformers, with loss categories as defined in [1].

Table II makes the evaluation based on the TOC, with the following data: $\mathrm{EP}=0.05 € / \mathrm{kWh}, \mathrm{n}=30$ years, $\mathrm{d}=7 \%$, $\mathrm{L}=0.5, \cos \phi=0.9$. It is concluded from Table II that the TOC ranking is different than the BP ranking.

Table III shows the savings due to the selection of S9 supplier (most expensive BP but lowest TOC) instead of S4 supplier (cheapest BP but highest TOC).

Table IV performs a sensitivity analysis of the electricity price when analyzing the savings due to the selection of S9 instead of S4 supplier.

Table I: Transformer offers

| Supplier | Rated power (kVA) | Bidding price $(€)$ | No-load losses (W) | Load losses $(\mathrm{W})$ | Loss category |
| :---: | :---: | :---: | :---: | :---: | :---: |
| S1 | 1,000 | 8,835 | 1,700 | 10,500 | $\mathrm{AA}^{\prime}$ |
| S2 | 1,000 | 9,410 | 1,400 | 10,500 | $\mathrm{AB}^{\prime}$ |
| S3 | 1,000 | 9,985 | 1,100 | 10,500 | $\mathrm{AC}^{\prime}$ |
| S4 | 1,000 | 8,395 | 1,700 | 13,000 | $\mathrm{BA}^{\prime}$ |
| S5 | 1,000 | 8,535 | 1,400 | 13,000 | $\mathrm{BB}^{\prime}$ |
| S6 | 1,000 | 8,640 | 1,100 | 13,000 | $\mathrm{BC}^{\prime}$ |
| S7 | 1,000 | 9,400 | 1,700 | 9,500 | $\mathrm{CA}^{\prime}$ |
| S8 | 1,000 | 9,535 | 1,400 | 9,500 | $\mathrm{CB}^{\prime}$ |
| S9 | 1,000 | 10,295 | 1,100 | 9,500 | $\mathrm{CC}^{\prime}$ |

Table II: Evaluation based on the total owning cost

|  | Efficiency | Wattage | Energy losses |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Supplier | $(\mathrm{n})$ | losses $(\mathrm{W})$ | NLL cost <br> $(\mathrm{kWh} / \mathrm{yr})$ | LL cost <br> $(€)$ | Cost of losses <br> $(€)$ | Total cost <br> $(€ / \mathrm{yr})$ | TOC <br> of losses $(€)$ | BP <br> $(€)$ | TOC <br> ranking | ranking |
| S1 | $99.05 \%$ | 4,325 | 37,887 | 9,887 | 15,266 | 1,894 | 25,153 | 33,988 | 4 | 7 |
| S2 | $99.11 \%$ | 4,025 | 35,259 | 8,142 | 15,266 | 1,763 | 23,408 | 32,818 | 6 | 4 |
| S3 | $99.18 \%$ | 3,725 | 32,631 | 6,397 | 15,266 | 1,632 | 21,663 | 31,648 | 8 | 3 |
| S4 | $98.91 \%$ | 4,950 | 43,362 | 9,887 | 18,901 | 2,168 | 28,787 | 37,182 | 1 | 9 |
| S5 | $98.98 \%$ | 4,650 | 40,734 | 8,142 | 18,901 | 2,037 | 27,043 | 35,578 | 2 | 8 |
| S6 | $99.04 \%$ | 4,350 | 38,106 | 6,397 | 18,901 | 1,905 | 25,298 | 33,938 | 3 | 6 |
| S7 | $99.10 \%$ | 4,075 | 35,697 | 9,887 | 13,812 | 1,785 | 23,699 | 33,099 | 5 | 5 |
| S8 | $99.17 \%$ | 3,775 | 33,069 | 8,142 | 13,812 | 1,653 | 21,954 | 31,489 | 7 | 2 |
| S9 | $99.23 \%$ | 3,475 | 30,441 | 6,397 | 13,812 | 1,522 | 20,209 | 30,504 | 9 | 1 |

Table III: Savings due to the selection of S 9 instead of S 4 supplier ( $\mathrm{EP}=0.05 € / \mathrm{kWh}$ )

| BP $(€)$ | n | Wattage <br> losses $(\mathrm{W})$ | Energy losses <br> $(\mathrm{kWh} / \mathrm{yr})$ | Cost of losses <br> $(€ / \mathrm{yr})$ | Simple <br> payback $(\mathrm{yr})$ | Total cost of <br> losses $(€)$ | TOC <br> $(€)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 646 | 2.94 | 8,578 | 6,678 |

Table IV: Savings due to the selection of S9 instead of S4 supplier (sensitivity analysis of electricity price)

| EP <br> $(€ / \mathrm{kWh})$ | $\mathrm{BP}(€)$ | n | Wattage <br> losses $(\mathrm{W})$ | Energy losses <br> $(\mathrm{kWh} / \mathrm{yr})$ | Cost of losses <br> $(€ / \mathrm{yr})$ | Simple <br> payback $(\mathrm{yr})$ | Total cost of <br> losses $(€)$ | TOC <br> $(€)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.04 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 517 | 3.68 | 6,862 | 4,962 |
| 0.05 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 646 | 2.94 | 8,578 | 6,678 |
| 0.06 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 775 | 2.45 | 10,294 | 8,394 |
| 0.07 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 904 | 2.10 | 12,009 | 10,109 |
| 0.08 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 1,034 | 1.84 | 13,725 | 11,825 |
| 0.09 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 1,163 | 1.63 | 15,440 | 13,540 |
| 0.10 | $-1,900$ | $0.33 \%$ | 1,475 | 12,921 | 1,292 | 1.47 | 17,156 | 15,256 |

## References

[1] CENELEC harmonization document 428.1 S1, 1992.

